

## Year 6

### Key Mathematical Concepts and representations

#### Number and Place Value

Year 6

#### Powers of 10 (1)

#### Vocabulary:

Tens Hundreds Thousands Ten-thousands Hundred-thousands Ones Digit Place Value Millions Ten-Millions Tenths Hundredths Represents Gattegno Tens Frame Equivalent Equation Multiply Divide Counters

One-tenth/hundredth times the size Ten/hundred times the size

| М    | illions | 3  | Th  | ousan | lds |     | Ones |    | -t | hs |
|------|---------|----|-----|-------|-----|-----|------|----|----|----|
| 100s | 10s     | 1s | 100 | 10s   | 1s  | 100 | 10s  | 1s |    |    |
|      |         |    | s   |       |     | s   |      |    |    |    |
|      |         |    |     |       |     |     |      | 0  | 0  | 1  |
|      |         |    |     |       |     |     |      | 0  | 1  |    |
|      |         |    |     |       |     |     |      | 1  |    |    |
|      |         |    |     |       |     |     | 1    | 0  |    |    |
|      |         |    |     |       |     | 1   | 0    | 0  |    |    |
|      |         |    |     |       | 1   | 0   | 0    | 0  |    |    |
|      |         |    |     | 1     | 0   | 0   | 0    | 0  |    |    |
|      |         |    | 1   | 0     | 0   | 0   | 0    | 0  |    |    |
|      |         | 1  | 0   | 0     | 0   | 0   | 0    | 0  |    |    |
|      | 1       | 0  | 0   | 0     | 0   | 0   | 0    | 0  |    |    |

| 1,000,000 | 2,000,000 | 3,000,000 | 4,000,000 | 5,000,000 | 6,000,000 | 7,000,000 | 8,000,000 | 9,000,000 |  |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|--|
| 100,000   | 200,000   | 300,000   | 400,000   | 500,000   | 600,000   | 700,000   | 800,000   | 900,000   |  |
| 10,000    | 20,000    | 30,000    | 40,000    | 50,000    | 60,000    | 70,000    | 80,000    | 90,000    |  |
| 1,000     | 2,000     | 3,000     | 4,000     | 5,000     | 6,000     | 7,000     | 8,000     | 9,000     |  |
| 100       | 200       | 300       | 400       | 500       | 600       | 700       | 800       | 900       |  |
| 10        | 20        | 30        | 40        | 50        | 60        | 70        | 80        | 90        |  |
| 1         | 2         | 3         | 4         | 5         | 6         | 7         | 8         | 9         |  |
| 0.1       | 0.2       | 0.3       | 0.4       | 0.5       | 0.6       | 0.7       | 0.8       | 0.9       |  |
| 0.01      | 0.02      | 0.03      | 0.04      | 0.05      | 0.06      | 0.07      | 0.08      | 0.09      |  |
|           |           |           |           |           |           |           |           |           |  |

|   |   |   |   |   |   |   |   |   | 0 | 0 | 1000 | 1 | one hundredth        |
|---|---|---|---|---|---|---|---|---|---|---|------|---|----------------------|
|   |   |   |   |   |   |   |   |   | 0 | 1 |      |   | one tenth            |
|   |   |   |   |   |   |   |   |   | 1 |   |      |   | one                  |
|   |   |   |   |   |   |   |   | 1 | 0 |   |      |   | ten                  |
|   |   |   |   |   |   |   | 1 | 0 | 0 |   |      |   | one hundred          |
|   |   |   |   |   | 1 | , | 0 | 0 | 0 |   |      |   | one thousand         |
|   |   |   |   | 1 | 0 | • | 0 | 0 | 0 |   |      |   | ten thousand         |
|   |   |   | 1 | 0 | 0 | , | 0 | 0 | 0 |   |      |   | one hundred thousand |
|   | 1 | , | 0 | 0 | 0 | e | 0 | 0 | 0 |   |      |   | one million          |
| 1 | 0 | , | 0 | 0 | 0 | , | 0 | 0 | 0 |   |      |   | ten million          |

Recognise that the 1 becomes ten times the size as it moves from right to left in a place value chart.

Recognise that 1 becomes one-tenth the size as it moves from left to right in a place value chart.

Recognise that the 1 becomes 10 times the size as it moves up in a Gattegno chart.

Recognise that 1 becomes one-tenth the size as it moves down in a Gattegno chart.



| Recognise that:                          |
|--|
| 10 hundredths are equivalent to 1 tenth. |
| 10 tenths are equivalent to 1 one.       |
| 10 ones are equivalent to 1 ten.         |

10 tens are equivalent to 1 hundred.

10 hundreds are equivalent to 1 thousand.

10 thousands are equivalent to 1 ten thousand.

10 ten thousands are equivalent to 1 hundred thousand.

10 hundred thousands are equivalent to 1 million.

10 millions are equivalent to 1 ten million.





| Number and Place Value | Vocabulary:  |
|------------------------|--|
| Year 6                 | Ones Tens Hundreds Thousands Ten-thousands Hundred-thousands<br>Millions Ten-Millions Tenths Hundredths Represents Digit Place Value |
| Powers of 10 (2)       | Counters Gattegno Tens Frame Equivalent Equation Multiply Divide   |
|                        | Ten/hundred times the size One-tenth/hundredth times the size  |

|   | 10,000,000 | 20,000,000 | 30,000,000 | 40,000,000 | 50,000,000 | 60,000,000 | 70,000,000 | 80,000,000 | 90,000,000 |
|---|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|   | 1,000,000  | 2,000,000  | 3,000,000  | 4,000,000  | 5,000,000  | 6,000,000  | 7,000,000  | 8,000,000  | 9,000,000  |
|   | 100,000    | 200,000    | 300,000    | 400,000    | 500,000    | 600,000    | 700,000    | 800,000    | 900,000    |
|   | 10,000     | 20,000     | 30,000     | 40,000     | 50,000     | 60,000     | 70,000     | 80,000     | 90,000     |
|   | 1,000      | 2,000      | 3,000      | 4,000      | 5,000      | 6,000      | 7,000      | 8,000      | 9,000      |
| ) | 100        | 200        | 300        | 400        | 500        | 600        | 700        | 800        | 900        |
| + | 10         | 20         | 30         | 40         | 50         | 60         | 70         | 80         | 90         |
|   | 1          | 2          | 3          | 4          | 5          | 6          | 7          | 8          | 9          |
| - | 0.1        | 0.2        | 0.3        | 0.4        | 0.5        | 0.6        | 0.7        | 0.8        | 0.9        |
|   | 0.01       | 0.02       | 0.03       | 0.04       | 0.05       | 0.06       | 0.07       | 0.08       | 0.09       |

Explore the Gattegno chart and recognise numbers that are one hundred times the size and one-hundredth times the size.

Ten is one hundred times the size of 0.1. 0.1 multiplied by 100 is equal to 10. 0.1 is one-hundredth of the size of 10. 10 divided by 100 is equal to 0.1.

|        | 1,000s | 100s | 10s | 1s | 0.1s | 0.01s | 0.001s |     |
|--------|--------|------|-----|----|------|-------|--------|-----|
|        |        |      | 2   | 5  |      |       |        |     |
| ÷ 100↓ |        |      | 0   | 0  | 2    | 5     |        | 1 × |

| 0.25 | × | 100 | = | 25   |
|------|---|-----|---|------|
| 25   | ÷ | 100 | = | 0.25 |

| 1,000 | 2,000 | 3,000 | 4,000 | 5,000 | 6,000 | 7,000 | 8,000 | 9,000 |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 100   | 200   | 300   | 400   | 500   | 600   | 700   | 800   | 900   |
| 10    | 20    | 30    | 40    | 50    | 60    | 70    | 80    | 90    |
| 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     |
| 0.1   | 0.2   | 0.3   | 0.4   | 0.5   | 0.6   | 0.7   | 0.8   | 0.9   |
| 0.01  | 0.02  | 0.03  | 0.04  | 0.05  | 0.06  | 0.07  | 0.08  | 0.09  |
| 0.001 | 0.002 | 0.003 | 0.004 | 0.005 | 0.006 | 0.007 | 0.008 | 0.009 |

Use the Place Value chart and Gattegno chart to support children to visualise multiplying and dividing by 10, 100 or 1000.

25 is one hundred times the size of 0.25. 0.25 multiplied by 100 is equal to 25. 0.25 is one-hundredth of the size of 25. 25 divided by 100 is equal to 0.25.

Scaling Models

#### Number and Place Value

#### Year 6

#### Place Value in Numbers up to 10,000,000.

#### Vocabulary:

Thousands Ten-thousands Hundred-thousands Ones Tens Hundreds Millions Ten-Millions Tenths Hundredths Represents Digit Place Value Gattegno Partition Combine Counters Equation Addend Sum Minuend Subtrahend Difference



Form numbers to 10,000,000 using place value counters and the part-part-whole model. The 2 represents 2 tens The 9 represents 9 hundreds The 3 represents 3 hundred thousands.

Write as an additive equation.

#### 200,000 + 10,000 + 100 + 20 = 210,120

| М    | lillion | 5  | Th   | ousan | nds | Ones |     |    |  |
|------|---------|----|------|-------|-----|------|-----|----|--|
| 100s | 10s     | 1s | 100s | 10s   | 1s  | 100s | 10s | 1s |  |
|      |         |    |      |       | 1   | 9    | 3   | 7  |  |
|      |         |    |      | 5     | 1   | 9    | 3   | 7  |  |
|      |         |    | 4    | 5     | 1   | 9    | 3   | 7  |  |
|      |         | 5  | 4    | 5     | 1   | 9    | 3   | 7  |  |

Read numbers to 10,000,000. Focus on the structure of millions, thousands and ones.

5 million, four hundred and fifty one thousand, nine hundred and thirty one (ones).

#### 30,051.2 1,000,000 2,000,000 4,000,000 5,000,000 6,000,000 7,000,000 8,000,000 9,000,000 100,000 200,000 300,000 400,000 500,000 600,000 700,000 800,000 9,000,000 100,000 200,000 300,000 400,000 500,000 600,000 700,000 800,000 9,000,000

30 thousand

| 100  | 0,000 | 200,000 | 300,000 | 400,000 | 500,000 | 600,000 | 700,000 | 800,000 | 900,000 |
|------|-------|---------|---------|---------|---------|---------|---------|---------|---------|
| 10   | 0,000 | 20,000  | 30,000  | 40,000  | 50,000  | 60,000  | 70,000  | 80,000  | 90,000  |
| 1    | ,000  | 2,000   | 3,000   | 4,000   | 5,000   | 6,000   | 7,000   | 8,000   | 9,000   |
| 1    | 100   | 200     | 300     | 400     | 500     | 600     | 700     | 800     | 900     |
|      | 10    | 20      | 30      | 40      | 50      | 60      | 70      | 80      | 90      |
| 2    | 1     | 2       | 3       | 4       | 5       | 6       | 7       | 8       | 9       |
| - 22 | 0.1   | 0.2     | 0.3     | 0.4     | 0.5     | 0.6     | 0.7     | 0.8     | 0.9     |
|      | 0.01  | 0.02    | 0.03    | 0.04    | 0.05    | 0.06    | 0.07    | 0.08    | 0.09    |

Make connections between different representations of numbers to 10,000,000 with the Gattegno Chart.

#### 3,870,291.46

| Ν           | Millions |      |     | Thousands |      |     | Ones |      |       |   |  |
|-------------|----------|------|-----|-----------|------|-----|------|------|-------|---|--|
| 100s 10s 1s |          | 100s | 10s | 1s        | 100s | 10s | 1s   | 0.1s | 0.01s |   |  |
|             |          | 3    | 8   | 7         | 0    | 2   | 9    | 1    | 4     | 6 |  |

Recognise the value of each digit. The 3 represent 3 million.



| Number and Place Value                       | Vocabulary:   |
|--|---|
| Year 6                                       | Ones Tens Hundreds Thousands Ten-thousands Hundred-thousands Millions Ten-Millions<br>Tenths Hundredths Represents Digit Place Value Intervals Scales Divisions |
| Reading Scales with 2, 4, 5, or 10 intervals | Equal Parts Whole Value Bar model Plus Minus Multiply Divide Grams<br>Millilitres Litres Grams Kilograms Metres Centimetres Estimate                            |



# Addition and Subtraction Year 6 Quantify additive and multiplicative relationships Additive Multiplicative Relationship Represents Compose Combine Total More than Less than Plus + Minus - Equal to = Addition Subtraction Divide ÷ Multiply x One-\_\_\_\_of Equation Expression Bar Model Whole Part Difference Multiplier Unknown Sequence Addend + Addend = Sum









| Addition and Subtraction                           | Vocabulary:   |  |
|--|---|--|
| Year 6   | AdditiveMultiplicativeRelationshipRepresentsComposeCombineTotalMore thanLess thanPlus +Minus -Equal to =AdditionSubtractionDivide ÷ |  |
| Quantify additive and multiplicative relationships | Multiply x Oneof Equation Expression Bar Model Whole Part<br>Difference Multiplier Unknown Sequence                                 |  |
|  | Addend + Addend = Sum   |  |

 $\frac{1}{3}$  of ?= 10



| 30 |    |    |
|----|----|----|
| 10 | 10 | 10 |

| whole by recognising   |  |  |
|------------------------|--|--|
| how many parts the     |  |  |
| vhole has been divided |  |  |
| into.                  |  |  |

$$\frac{1}{3}$$
 of 30 = 10







ь

b

one part = 20 ÷ 5 = 4

b = 4

a = 4 × 4 = 16

The two numbers are 9 and 16.

a = 9 + 7 = 16

The two numbers are 16 and 4.



÷ 100

÷ 100

- 0.4

0.4 \_

| Addition, Subtraction, Multiplication and Division | Vocabulary:  |  |
|--|--|--|
| Year 6   | Additive Multiplicative Relationship Represents Compose Combine<br>Total   |  |
| Quantify additive and multiplicative relationships | More than       Less than       Plus +       Minus -       Equal to =       Addition       Subtraction       Divide         ÷ Multiply x       Oneof       Equation       Expression       Bar Model       Whole         Part Difference       Multiplier         Unknown       Sequence |  |
| $\frac{1}{3}$ of ?= 10                             | Addend + Addend = SumFactor x Factor = Product (Multiplicand x Multiplier = Product)Minuend - Subtrahend = DifferenceDividend ÷ Divisor = Quotient   |  |



 $\frac{1}{3}$  of 30 = 10



#### **Addition and Subtraction**

#### Year 6

#### Solve Problems involving Ratio Relationship

#### Vocabulary:

AdditiveMultiplicativeRelationshipRepresentsEquationUnknownScale-factorRatioRatioTable\_\_\_\_\_\_\_times the sizeone-\_\_\_\_\_the size ofVertical Horizontal

Factor x Factor = Product (Multiplicand x Multiplier = Product)

Dividend ÷ Divisor = Quotient





The two numbers are 9 and 16.

The two numbers are 16 and 4.

#### **Fractions**

Year 6

#### **Simplify Fractions**

#### Vocabulary:

FractionNotationDividedEqualNumeratorDenominatorWholePartsFraction Bar (Vinculum)HalfThirdQuarterFifthSixthSeventhEighthNinthTenthOne-\_\_\_\_MultipleFactorCommonSimplifySimplest FormMixed NumberImproper FractionHighest Common Factor





Recap equivalent fractions with multiple representations. Identify a fraction in its simplest form when the only common multiple of both the numerator and denominator is 1.

 $\frac{1}{4}$  is in its simplest form. I know this because the only common factor of the numerator and the denominator is 1.



8

÷2

÷2

<u>4</u> 12

÷4

 $\div 4$ 

3

12

9

12

12

16

÷1

÷1

12

 $\frac{4}{12}$ 

 $\frac{2}{6}$ 

Extend to fractions where the numerator in the simplest form is greater than 1.  $\frac{3}{4}$  is in its simplest form. I know this because the only common factor of the numerator and the

denominator is 1.

Finding the common factors of both the numerator and denominator allows us to simplify each fraction to its simplest form.

The common factors of 4 and 12 are 1, 2 and 4.

#### The highest common factor is 4.

#### Generalisation:

Dividing both the numerator and the denominator of a fraction by their highest common factor converts the fraction to its simplest form.





Improper fraction can be simplified before or after they are converted to a mixed number. The highest common factor of 20 and 12 is 4. The highest common factor of 8 and 12 is 4.



÷4

=

÷4

<u>5</u> 3

<u>20</u> 12



#### **Fractions**

#### Year 6

#### **Compare Fractions with Different Denominators**

Vocabulary: Fraction Notation Divided Equal Numerator Denominator Whole Parts Fraction Bar (Vinculum) Half Third Quarter Fifth Sixth Seventh Multiple Common Denominator Ninth Tenth One-\_\_\_ Convert Express

Proportion Estimate Position Number Line Greater than Less than





**Generalisations:** 

*If the numerators are both 1, then the larger the denominator,* 

the smaller the fraction.

The denominator represents the number of equal parts the

whole has been split into. The greater this number, the more

equal parts and therefore the smaller the size of each part.

is about here. I imagined the line divided into 4 equal parts and then pictured 3 of them. 3 is quite

a big part of 4, so  $\frac{3}{4}$  is nearer to 1.

 $\frac{1}{3}$ 34

is about here. I imagined the

ne divided into 3 equal parts.





We can compare fractions and mixed numbers with the same numerator in different ways



 $\frac{7}{11} < \frac{5}{6}$ 

0

We can use our knowledge of fractions on a number line to help estimate and compare their relative size.



Eighth

Comparing their position in relation to the nearest landmark. How close is it to 1 whole? How close is it to 0? How close is it from  $\frac{1}{2}$ ?

We can reason about the proportional size of the numerator in relation to the denominator to compare fractions. 5 is a larger part of 6 than 7 is of 11, which means  $\frac{5}{6}$ is greater than  $\frac{7}{11}$ 

11

5 6